

Computational Approaches Towards Monotonicity in Sentence-Picture Verification

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Joint work with Marcin Zajenkowski
TLS 13



NL determiners

1. **All** poets have low self-esteem.
2. **Some** dean danced nude on the table.
3. **At least 3** grad students prepared presentations.
4. **An even number** of the students saw a ghost.
5. **Most** of the students think they are smart.
6. **Less than half** of the students received good marks.

Monotone quantifiers

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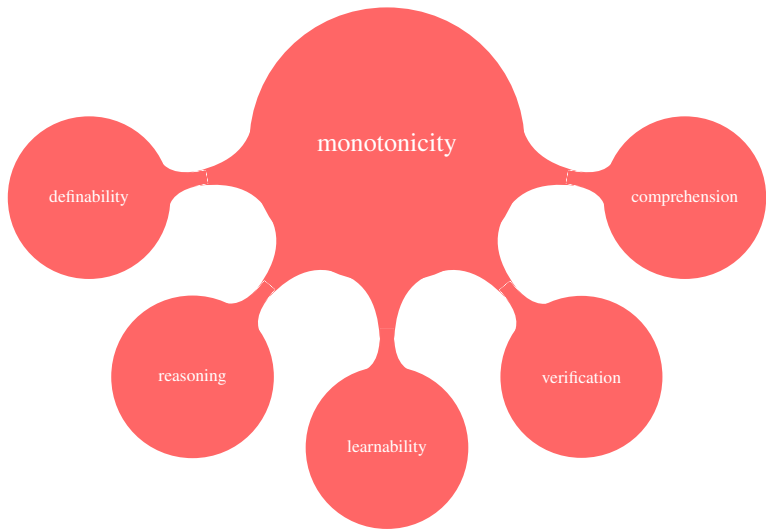
Definition

Q is decreasing iff, for any $A \subseteq A'$, $Q(A', B)$ entails $Q(A, B)$.

Example

1. No child is dirty.
2. No boy is dirty.

Monotonicity – key property in logic and language



Barwise and Cooper's observation

Observation

Monotonicity relates to verification procedures.

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Example (witness set)

1. Some cars are green.
2. No cars are red.



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Hypothesis

'Response latencies for verification tasks involving decreasing quantifiers would be somewhat greater than for increasing quantifiers' (p. 192).



Barwise and Cooper, Generalized Quantifiers and Natural Language, Linguistics and Philosophy, 1981

Truth-values??

Question

What about truth-value?

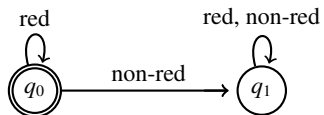
Simplicity

- ▶ Simple quantifiers can be computed by simple automata.
- ▶ Encoding natural counting strategies.
- ▶ We restrict ourselves to precise counting.

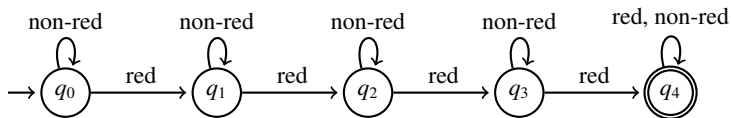


Van Benthem, Essays in logical semantics, 1986

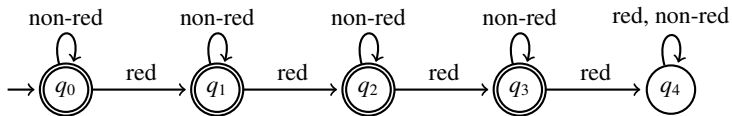
Every dot is red.



More than 3 dots are red.



Fewer than 4 dots are red.



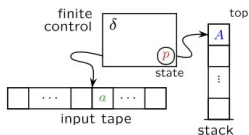
Proportional quantifiers

1. More than half of the dots are red.
2. Fewer than half of the dots are red.



Proportional quantifiers

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- ▶ Not computable by finite-automata.
- ▶ We need working memory.
- ▶ Simple push-down automata will do.

Observation

The more complex automata the longer RT and the greater WM involvement.



McMillan et al., Neural basis for generalized quantifiers comprehension, *Neuropsychologia*, 2005



Szymaniki & Zajenkowski, Comprehension of simple quantifiers. Empirical evaluation of a computational model, *Cognitive Science*, 2010



Zajenkowski et al., A computational approach to quantifiers as an explanation for some language impairments in schizophrenia, *JCD*, 2011

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- ▶ Subjects were timed when asked to decide if true.
- ▶ Reading and verification time.

Predictions

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2. Complexity influenced by (monotonicity \times truth-value):
 - ▶ In the case of the cardinal sentences,
 - ▶ but not the proportional sentences.

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4. Proportional quantifiers > cardinal quantifiers.

- ▶ 61 native Polish-speaking adults (33 female).
- ▶ Volunteers: undergraduates from the University of Warsaw.
- ▶ The mean age: 21.42 years ($SD = 3.22$).
- ▶ Each participant tested individually.

16 grammatically simple propositions in Polish, like:

1. More than 7 cars are blue.
2. Fewer than 8 cars are yellow.
3. More than half of the cars are red.
4. Fewer than half of the cars are black.

More than half of the cars are yellow.



An example of a stimulus used in the first study

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- ▶ Reading and verification stages.
- ▶ **Cardinal and proportional quantifiers were equivalent.**

Reading times were similar

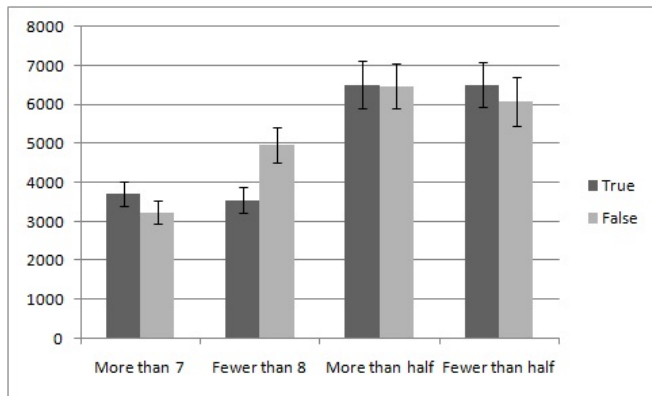
Quantifier	M	SD
More than 7	3430	1497
Fewer than 8	3577	1793
More than half	3695	1698
Fewer than half	3908	1639

Verification times

Quantifier		M	SD
More than 7	True	3710	1230
	False	3241	1167
	Overall	3475	955
Fewer than 8	True	3564	1311
	False	4971	1843
	Overall	4259	1312
More than half	True	6511	2454
	False	6475	2195
	Overall	6493	1959
Fewer than half	True	6509	2378
	False	6084	2464
	Overall	6296	2090



Interaction effect



False/True interaction

Refinement on Barwise & Cooper.



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Take home message

- ▶ Complexity influences verification
- ▶ Monotonicity \times truth-value influences complexity



Thanks!



Observation

Processing time of negative quantifiers is greater than processing time of affirmative quantifiers.



Just & Carpenter, Comprehension of negation with quantification, Journal of Verbal Learning and Verbal Behavior, 1971

3 kinds of sentences

1. Syntactic negatives with particle:

- ▶ The dots are red.
- ▶ The dots aren't red.

2. Syntactic negatives without particle:

- ▶ Many of the dots are red.
- ▶ Few of the dots are red.

3. Semantic negatives:

- ▶ A majority of the dots are red.
- ▶ A minority of the dots are red.

Only some pairs contrasted w.r.t. monotonicity:

1. All of the dots are red.
2. None of the dots are red.

Most of the material was based on negativity vs. affirmativity.

Negativity is Marked, not only linguistically

Example

How tall are you? **but not** How short are you?

Example (Squirrel Monkeys)



1. If everything is black, choose the biggest object.
2. If everything is white, choose the smallest object.

Once trained, monkey were consistently faster in task 1.



McGonigle and Chalmers, The Ontology of Order, 1996

Affirmativity and monotonicity?

- ▶ Monotonicity is a semantic property of quantifiers;
- ▶ Degree of affirmativity is a linguistic concept, e.g.:
 - ▶ tag test;
 - ▶ licensing NPIs.

Example

1. Few children are dirty, are they?
2. Few children believe that any more.
3. *A few children are dirty, are they?
4. *A few children believe that any more.

Comparison Model

4 stage processing of the comparison model:

1. sentence encoding,
2. picture encoding,
3. comparing,
4. responding.

Component latencies are additive.

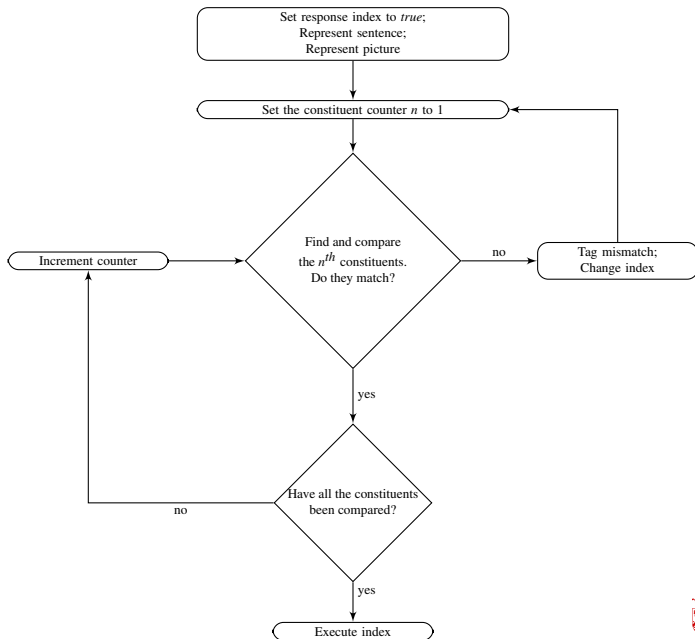


Clark & Chase, On the Process of Comparing Sentences Against Pictures, Cognitive Psychology, 1972

Example: The Dots are (not) White.

True affirmative		False affirmative	
Comparison:	Index	Comparison:	Index
<i>Aff</i> (white, dots)	<i>true</i>	<i>Aff</i> (white, dots)	<i>false</i>
<i>Aff</i> (white, dots)		<i>Aff</i> (black, dots)	
+		-	
+		+	
2 comparisons		3 comparisons	
True negative		False negative	
Comparison:	Index	Comparison:	Index
<i>Neg</i> (white, dots)	<i>false</i>	<i>Neg</i> (white, dots)	<i>false</i>
<i>Aff</i> (white, dots)		<i>Aff</i> (black, dots)	
-		-	
+		+	
4 comparisons		5 comparisons	

Computational Model



Pros & Cons of the Comparison Model

Pros

- ▶ *Explains variations w.r.t. negativity:*
 - ▶ *negatives harder than affirmatives;*
 - ▶ *true affirmatives easier than false ones;*
 - ▶ *false negatives easier than true ones.*

Cons

- ▶ *It says very little about monotonicity.*
- ▶ *Arbitrary psychological/linguistic representation.*
- ▶ *Little insight into the actual computational process.*
- ▶ *At best, post-hoc theory for the specific task.*



Tanenhaus et al., Sentence-Picture Verification Models as Theories of Sentence Comprehension: A Critique of Carpenter and Just, Psychological Review, 1976

Question

How to cover generalized quantifiers?